





name of the unit:		symbol:
THE DIVISION OF INSURANCE		I-73
AND CAPITAL MARKETS		http://www.im.p.lodz.pl
Institute of Mathematics, Lodz University of Technology		
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scope of activities: Research activities are carried out in two directions:		graphic material
 The first one concerns modeling of insurer's solvency in switching models, evaluation of ruin probability, time to ruin, deficit size, etc., as well as estimation of model's parameters. The second direction is related to interest rate risk in long-term insurance, methods of pricing and hedging against this risk. 		
present activities: Ad. 1. Both numerical and theoretical approaches are being developed to investigate switching models. The main theoretical tool is the risk operator approach introduced in Gajek (2005). Based on the properties of the risk operator, we evaluate ruin probability, time to ruin, deficit size, etc. Ad. 2. New evaluations of the VaR measure of the change in portfolio surplus due to the change of the term structure of interest rates are investigated. The bounds are supposed to be products of two terms: the one depending on the portfolio structure and the second depending on the interest rate change measure. The measure is related to the L _P -distance in the space of financial instruments. We investigate its relationship with other measures, like M ² . Explicit formulas for some life insurance products are obtained. Optimal streams of assets are investigated under several restrictions imposed on e.g. duration, M ² or other parameters of the asset flow. The influence of the lack of short sale on the efficiency of the interest rate risk protection is investigated.		$\Psi(u) \leqslant e^{-ru}$ $\Psi(u, yu) \leqslant e^{-ryu}$

We plan to investigate the risk switching models in the uncertain environment when the switch's parameters are partly known and partly unknown. This approach will be also useful when life-insurance products are analysed from a long time perspective and we plan to explore it in this context as well.







Publications/patents, awards, projects:

- Lesław Gajek, On the deficit distribution when the ruin occurs-discrete time model, Insurance: Mathematics and Economics 36 (2005), 13-24
- Lesław Gajek, Marcin Rudź, Banach Contraction Principle and ruin probabilities in regime-switching models, Insurance: Mathematics & Economics 80 (2018) 45-53
- Lesław Gajek, Elżbieta Krajewska, Balance-sheet interest rate risk: a weighted L^p approach, Journal of Risk 21 (2018) 91-104
- Lesław Gajek, Marcin Rudź, Finite-Horizon Ruin Probabilities in a Risk-Switching Sparre Andersen Model, Methodology and Computing in Applied Probability, 22 (2020) 1493-1506
- Lesław Gajek, Łukasz Kuciński, Complete discounted cash flow valuation, Insurance: Mathematics & Economics 73 (2017) 1-19
- Lesław Gajek, Marcin Rudź, Sharp approximations of ruin probabilities in the discrete time models, Scand. Actuar. J. 5 (2013) 352-382
- Lesław Gajek, Elżbieta Krajewska, A new immunization inequality for random streams of assets, liabilities and interest rates, Insurance: Mathematics and Economics 53 (2013) 624-631
- Marek Kałuszka, Andrzej Okolewski, A note on multiple life premiums for dependent lifetimes, Insurance: Mathematics and Economics 57 (2014), 25-30

Keywords:

insurer's solvency; risk switching models; ruin probability; time to ruin; deficit size; estimation of model's parameters; term structure of interest rates; VaR ; M2-measure; portfolio optimization

List of internship proposal in this research team:

Risk management in insurance.